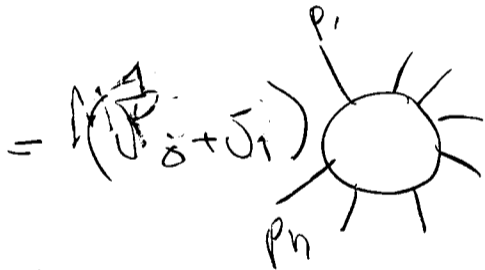
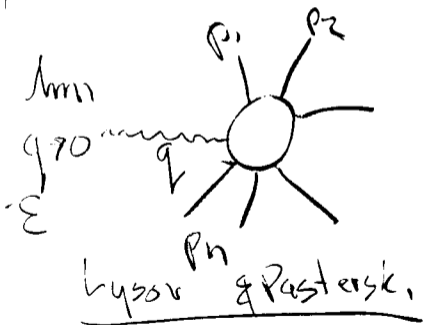


Soft theorem
 \Leftrightarrow asymptotics



infinitesimal
 $=$ symmetry

QED $\mathcal{J}_0 = \sum_{k=1}^N e_k \frac{\epsilon \cdot p_k}{q \cdot p_k}$

QED $\mathcal{J}_0, \mathcal{J}_1$

YM $\mathcal{J}_0, \mathcal{J}_1$

Gravity $\mathcal{S}_0, \mathcal{S}_1, \mathcal{S}_2$

$\mathcal{T}(S) = 0$

susy

other dimens.

1. Minkowski spacetime \leftrightarrow string theory

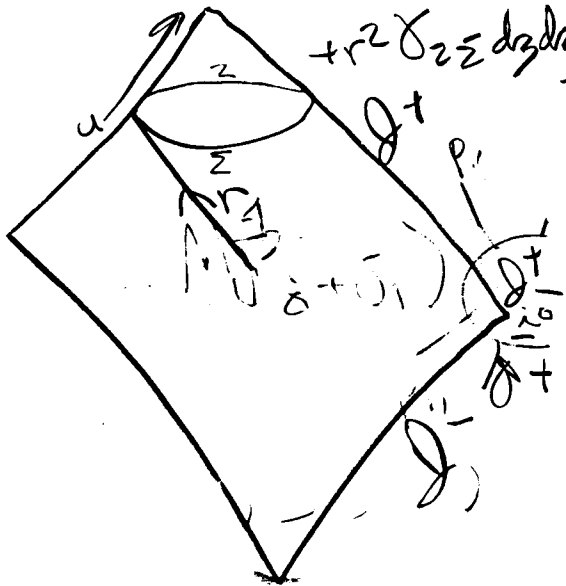
2. Reorganize/improve \mathcal{J}_k comp for collider physics

3. Insight into amplitudes/functors

Asymptotic Symmetries

$$ds^2 = -du^2 - 2du dr$$

$$+ r^2 \delta_{\bar{z}\bar{z}} dz d\bar{z}$$



$$\nabla^M F_{uv} = j^M$$

$$A_r = 0$$

$$A_u|_{J^+} = 0$$

$$A_z = \underline{A_z(u, z, \bar{z})} +$$

$$\left(u = \frac{1}{r} A_u(u, z, \bar{z}) + \mathcal{O}\left(\frac{1}{r^2}\right) \right)$$

$$\delta_{z\bar{z}} \partial_u A_u = \partial_u (\partial_z A_{\bar{z}} + \partial_{\bar{z}} A_z) + e^2 \delta_{z\bar{z}} g_u = 0$$

$$\delta A_z = \partial_z \epsilon(z, \bar{z})$$

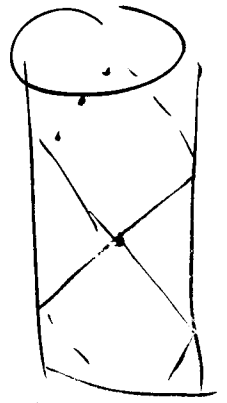
$$Q_\epsilon^+ = \int_{\mathcal{S}^1} d^2z \epsilon F_{ru} = \int_{\mathcal{S}^1} \partial_u (\partial_z A_{\bar{z}} + \partial_{\bar{z}} A_z + \delta_{z\bar{z}} \delta u) = \overline{Q_\epsilon}$$

$A(u, z, \bar{z}) + \dots$

$$\delta B_z = \partial_z \epsilon^-$$

$$\boxed{\epsilon(z, \bar{z}) = \epsilon^-(z, \bar{z})}$$

$$[Q_\epsilon, S] = 0$$



$$\langle \text{contour} \int_{\gamma} (A(z) dz) \rangle_{\text{form}} = 0$$

$$\varepsilon(z) = \frac{1}{z - a}$$

$$f(z) = (p_1 \dots p_n)$$

$$\int \sum_k \frac{\varepsilon \cdot p_k}{p_k} \chi(p_1 \dots p_n)$$